# U sing theoretical descriptors in quantitative structure- property relationships: gas phase acidity of some hydrocarbons and nitrohydrocarbons 



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#### Abstract

C alculation of the gas phase acidity of some hydrocarbons and nitrohydrocarbons is studied using direct (quantum mechanical) methods as well as a model equation, derived with the aid of correlation analysis, relating empirical values to computational molecular parameters. A greement between directly calculated and empirical values is improved by correlation equations. T he correlation analysis model is statistically significant and physically reasonable; gas phase acidity increases with acidity modelling parameters and decreases with basicity modelling parameters.


## Introduction

This study is based on an interest in 'energetic' (small, strained, easily oxidizable) molecules and the need to predict their properties. In principle, properties may be predicted using direct (quantum mechanical) methods as well as equations derived with the aid of correlation analysis. This study explores the use of direct and correlation analysis methods to calculate a property, gas phase acidity, directly amenable to these methods. The gas phase acidity, defined as $\Delta_{\mathrm{a}} \mathrm{H}$ or $\Delta_{\mathrm{a}} \mathrm{G}$ for the process in eqn. (1), can be directly found from first principles (semiempirical

$$
\begin{equation*}
\mathrm{RH}(\mathrm{~g})=\mathrm{R}^{-}(\mathrm{g})+\mathrm{H}^{+}(\mathrm{g}) ; \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{RH}) \tag{1}
\end{equation*}
$$

and ab initio quantum mechanical methods) through calculation of the heats of formation of the species; $\Delta_{\mathrm{a}} \mathrm{H}(\mathrm{RH})=\Delta_{\mathrm{f}} \mathrm{H}$ -$\left(\mathrm{R}^{-}\right)+\Delta_{\mathrm{f}} \mathrm{H}\left(\mathrm{H}^{+}\right)-\Delta_{\mathrm{f}} \mathrm{H}(\mathrm{RH})$. (N ote that increasing $\Delta_{\mathrm{a}} \mathrm{H}$ implies decreasing conventional acidity.) In addition, theoretical calculations have been done for a number of compounds using ab initio and semiempirical quantum mechanical methods. Often, such calculated results are more useful for examining trends rather than providing exact values. Ab initio results depend on the basis set and the level of theory. Diffuse functions are required for the anion calculations, and sometimes result in linear dependence which makes convergence of H artree-Fock equations difficult. ${ }^{1} \Delta_{\mathrm{a}} \mathrm{H}$ has been measured for a large number of compounds; as a result there is a large NIST Standard Reference D atabase. ${ }^{2}$

The existence of empirical values for a set of compounds permits the use of correlation analysis (statistics) to find coef-
ficients in an equation relating empirical property values to a set of molecular parameters. This approach has been used in quantitative structure-activity (property) relationships (QSAR, QSPR ) in which measured bulk properties have been correlated with predominantly empirical molecular structural parameters. $U$ sing experiment, statistics and theory may seem to lack rigour in describing nature but Otto Exner's statement, 'any regularity found in nature raises some kind of satisfaction ${ }^{3}$ is appropriate. Hansch, ${ }^{4}$ K amlet, Taft and Abraham (KTA) ${ }^{5}$ have extended linear free energy relationship (LFER) type work, ${ }^{6}$ a subset of QSAR, to involve solute-solvent interactions. ${ }^{7}$ The resulting model, a linear solvation energy relationship (LSER ), has used an empirical solvatochromatic (KTA) descriptor set and a more recently developed solvation parameter set to give successful correlations for well over 200 properties. ${ }^{8}$

Based on, and complementary to, the LSER philosophy, a set of molecular theoretical linear solvation energy relationship (TLSER) descriptors (computational) has been developed. These have shown good correlations and physical interpretations for many properties ${ }^{9-15}$ By their very nature, theoretical descriptors can give near a priori predictions; their calculations (and interpretations) are straightforward. Eqn. (2) gives one

$$
\begin{equation*}
\log P=a V_{m c}+b \pi_{1}+c \varepsilon_{\mathbf{B}}+d q_{-}+e \varepsilon_{A_{A}}+f q_{+}+\log P_{0} \tag{2}
\end{equation*}
$$

form of an LSER equation in terms of the TLSER parameters for some property, $\mathrm{P} ; \log \mathrm{P}_{0}$ represents an intercept. In this paper, $\Delta_{\mathrm{a}} \mathrm{G}$ and $\Delta_{\mathrm{a}} \mathrm{H}$ are used in place of $\log \mathrm{P}$ since these are direct energy quantities. Often, P is related to an equilibrium or rate constant, K ; hence, In K is linearly related to a free energy.

Table 1 TLSER descriptors

| Symbol | N ame | D efinition | $U$ nits ${ }^{\text {a }}$ | R ange |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{V}_{\mathrm{mc}}$ | M olecular volume | M olecular volume | $100 \AA^{3}$ | 0.3-3 |
| $\pi_{1}$ | Polarizability index | Polarizability $/ \mathrm{V}_{\text {mc }}$ | none | 0.07-0.16 |
| $\varepsilon_{\text {B }}$ | 'Covalent' H B basicity | 0.30-0.01( $\mathrm{E}_{\text {lw }}-\mathrm{E}_{\mathrm{h}}$ ) | heV | 0.1-0.17 |
| q- | 'Electrostatic' H B basicity | M aximum \|(-) chargel on an atom | acu | 0-0.8 |
| $\varepsilon_{\text {A }}$ | 'Covalent' H B acidity | 0.30-0.01( $\mathrm{E}_{1}-\mathrm{E}_{\text {hw }}$ ) | hev | 0.14-0.2 |
| $\mathrm{q}_{+}$ | 'Electrostatic' HB acidity | M aximum ( + ) charge on an H atom | acu | 0-0.8 |

[^0] energy; $\mathrm{E}_{\mathrm{h}}=\mathrm{HOM}$ O energy; $\mathrm{E}_{\mathrm{lw}}$ and $\mathrm{E}_{\mathrm{hw}}$ refer to the $\mathrm{E}_{\mathrm{l}}=5.4428 \mathrm{eV}$ and $\mathrm{E}_{\mathrm{h}}=-12.1911 \mathrm{eV}$ for water, respectively; ||indicate absolute magnitudes.

Table 2 Compounds with TLSER descriptors and empirical $\Delta_{\mathrm{a}} \mathrm{G}$ and $\Delta_{\mathrm{a}} \mathrm{H}$ values ( $\mathrm{kJ} \mathrm{mol}{ }^{-1}$ ) at 298 K ; compounds used in the direct semiempirical calculations for $\Delta_{\mathrm{a}} \mathrm{H}$ (Table 5) are marked with an asterisk (*)

| A cidic $\mathrm{H}^{\text {a }}$ | M olecule | $\mathrm{V}_{\mathrm{mc}}$ | $\pi_{1}$ | $\varepsilon_{B}$ | q- | $\varepsilon_{\text {A }}$ | $\mathrm{q}_{+}$ | $\Delta_{\mathrm{a}} \mathrm{G} / \mathrm{kJ} \mathrm{mol}^{-1}$ | $\Delta_{\mathrm{a}} \mathrm{H} / \mathrm{kJ} \mathrm{mol}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Nitric acid* | 0.3250 | 0.1190 | 0.1223 | 0.3483 | 0.1861 | 0.2380 | 1329.7 | 1357.7 |
| C12 | Fluoradene | 2.1263 | 0.1584 | 0.1601 | 0.0980 | 0.1832 | 0.0629 | 1359.4 | 1391.6 |
| C1 | 1,3-D iphenylindene* | 2.5669 | 0.1437 | 0.1581 | 0.0905 | 0.1794 | 0.0748 | 1375.7 | 1402.9 |
| C1 | 1,2,3-Triphenylindene | 3.1988 | 0.1482 | 0.1586 | 0.0901 | 0.1801 | 0.0642 | 1373.2 | 1404.2 |
| C3 | 2-Phenyl-5-p-tolylcyclopentadiene | 2.2264 | 0.1461 | 0.1557 | 0.1015 | 0.1772 | 0.0743 | 1381.1 | 1412.5 |
| C3 | 2,5-D iphenylcyclopentadiene | 2.0717 | 0.1458 | 0.1558 | 0.1006 | 0.1771 | 0.0742 | 1382.8 | 1412.9 |
|  | $N$ itrous acid | 0.2767 | 0.1001 | 0.1239 | 0.2496 | 0.1800 | 0.2032 | 1391.6 | 1423.8 |
| C9 | 9-Phenylfluorene | 2.3265 | 0.1438 | 0.1596 | 0.0826 | 0.1818 | 0.0629 | 1403.7 | 1436.4 |
| C9 | 9-N eopentylfluorene | 23701 | 0.1356 | 0.1595 | 0.1026 | 0.1818 | 0.0617 | 1419.2 | 1451.8 |
| C9 | 9-I sobutylfluorene | 2.2496 | 1.1347 | 0.1595 | 0.0808 | 0.1818 | 0.0616 | 1435.1 | 1467.7 |
| C9 | 9-M ethylfluorene | 1.6875 | 0.1475 | 0.1596 | 0.0810 | 0.1818 | 0.0616 | 1437.2 | 1468.2 |
| C9 | 9-tert-Butylfluorene | 2.2719 | 0.1341 | 0.1597 | 0.0864 | 0.1819 | 0.0618 | 1437.6 | 1468.6 |
| C9 | 9-E thylfluorene | 1.9069 | 0.1405 | 0.1596 | 0.0818 | 0.1818 | 0.0616 | 1436.8 | 1469.4 |
| C9 | 9-I sopropylfluorene | 2.0524 | 0.1394 | 0.1596 | 0.0386 | 0.1818 | 0.0616 | 1437.2 | 1469.8 |
| C9 | Fluorene* | 1.5606 | 0.1475 | 0.1595 | 0.0940 | 0.1818 | 0.0616 | 1439.3 | 1471.9 |
| C1 | Indene | 1.1307 | 0.1370 | 0.1580 | 0.1100 | 0.1793 | 0.0730 | 1441.8 | 1472.8 |
| $\mathrm{CH}_{3}$ | 4-N itrotoluene* | 1.1348 | 0.1362 | 0.1427 | 0.3298 | 0.1872 | 0.0858 | 1444.7 | 1474.9 |
| C9 | 2-M ethylfluorene | 1.7758 | 0.1431 | 0.1598 | 0.0996 | 0.1824 | 0.0618 | 1442.6 | 1475.3 |
| $\mathrm{CH}_{3}$ | 6,6-D imethylfulvene | 1.2171 | 0.1247 | 0.1565 | 0.0798 | 0.1841 | 0.0723 | 1453.9 | 1481.6 |
| C4 | N itrobenzene* | 0.9644 | 0.1375 | 0.1425 | 0.3288 | 0.1860 | 0.0851 | 1449.8 | 1482.0 |
| C1 | N itro-2,2-dimethylpropane | 1.1326 | 0.1118 | 0.1314 | 0.3368 | 0.1804 | 0.0519 | 1457.7 | 1486.2 |
| C1 | N itroethane* | 0.6204 | 0.1145 | 0.1308 | 0.3353 | 0.1808 | 0.0557 | 1462.3 | 1489.5 |
|  | N itroethyne | 0.4735 | 0.1233 | 0.1283 | 0.3142 | 0.1887 | 0.1829 | 1456.9 | 1489.5 |
| C2 | 2-N itropropane | 0.7967 | 0.1130 | 0.1314 | 0.3372 | 0.1799 | 0.0615 | 1464.4 | 1489.9 |
| $\mathrm{CH}_{3}$ | 2-N itrotoluene* | 1.1241 | 0.1362 | 0.1440 | 0.3297 | 0.1861 | 0.0848 | 1458.5 | 1489.9 |
|  | N itromethane* | 0.4495 | 0.1151 | 0.1302 | 0.3348 | 0.1818 | 0.0498 | 1463.1 | 1491.2 |
|  | Triphenylmethane* | 2.3784 | 0.1383 | 0.1540 | 0.0794 | 0.1760 | 0.0603 | 1467.3 | 1500.8 |
| C5 | Pentamethylcyclopentadiene | 1.5310 | 0.1212 | 0.1574 | 0.1266 | 0.1776 | 0.0350 | 1485.3 | 1509.6 |
| C1 | $N$ itroethene | 0.5616 | 0.1206 | 0.1312 | 0.3465 | 0.1882 | 0.1147 | 1482.8 | 1514.6 |
| $\mathrm{CH}_{3}$ | 9-M ethylanthracene | 1.8081 | 0.1604 | 0.1654 | 0.0617 | 0.1872 | 0.0613 | 1485.7 | 1515.4 |
| $\mathrm{CH}_{3}$ | 3-N itrotoluene* | 1.1128 | 0.1383 | 0.1439 | 0.3290 | 0.1860 | 0.0854 | 1488.2 | 1518.4 |
|  | D iphenylmethane | 1.7133 | 0.1301 | 0.1533 | 0.0879 | 0.1763 | 0.0600 | 1498.7 | 1521.3 |
| C1 | N itrocyclopropane | 0.6836 | 0.1230 | 0.1310 | 0.3322 | 0.1807 | 0.0996 | 1509.2 | 1534.3 |
| C1 | 1-Phenylprop-2-ene* | 1.2433 | 0.1279 | 0.1528 | 0.1155 | 0.1756 | 0.0599 | 1512.6 | 1540.1 |
| C1,2 | Penta-1,4-diene* | 0.8050 | 0.1163 | 0.1464 | 0.1147 | 0.1679 | 0.0496 | 1524.2 | 1544.7 |
|  | Phenylethyne | 0.9919 | 0.1396 | 0.1551 | 0.1251 | 0.1786 | 0.1581 | 1518.4 | 1551.0 |
| C1,2 | Cyclohexa-1,3-diene | 0.9149 | 0.1169 | 0.1561 | 0.0938 | 0.1758 | 0.0579 | 1530.5 | 1561.9 |
| $\mathrm{CH}_{3}$ | 1-M ethylnaphthalene | 1.3470 | 0.1475 | 0.1601 | 0.0831 | 0.1820 | 0.0608 | 1530.5 | 1565.2 |
| C7 | Cycloheptatriene | 0.9877 | 0.1267 | 0.1578 | 0.1046 | 0.1799 | 0.0678 | 1544.7 | 1569.8 |
| C5 | Cyclooctadiene | 1.2243 | 0.1206 | 0.1539 | 0.0877 | 0.1747 | 0.0487 | 1548.5 | 1576.1 |
| C1 | 3,3-D imethylbutyne | 0.9959 | 0.1067 | 0.1389 | 0.1653 | 0.1588 | 0.1570 | 1548.9 | 1581.6 |
|  | Ethyne* | 0.3248 | 0.0841 | 0.1355 | 0.1546 | 0.1568 | 0.1546 | 1547.2 | 1581.6 |
| C3 | Benzyne | 0.7252 | 0.1299 | 0.1499 | 0.1137 | 0.1822 | 0.0832 | 1552.3 | 1584.5 |
| C2 | 2-Phenylpropane | 1.2978 | 0.1241 | 0.1527 | 0.0759 | 0.1755 | 0.0602 | 1560.2 | 1585.7 |
| C4 | Bicyclo[3.2.1]octa-2,6-diene | 1.0960 | 0.1202 | 0.1498 | 0.1027 | 0.1695 | 0.0752 | 1559.0 | 1588.2 |
| C1 | Phenylethane* | 1.1783 | 0.1206 | 0.1528 | 0.0880 | 0.1755 | 0.0599 | 1561.9 | 1589.1 |
| C1 | Pentyne | 0.8625 | 0.1020 | 0.1387 | 0.1787 | 0.1595 | 0.1564 | 1556.4 | 1589.1 |
|  | Propadiene | 0.5090 | 0.1112 | 0.1454 | 0.2047 | 0.1668 | 0.0474 | 1556.4 | 1592.4 |
| $\mathrm{CH}_{3}$ | Toluene* | 0.9721 | 0.1266 | 0.1528 | 0.1007 | 0.1756 | 0.0598 | 1563.6 | 1593.3 |
| C1 | Propyne | 0.4767 | 0.1035 | 0.1384 | 0.1874 | 0.1597 | 0.1562 | 1561.9 | 1594.5 |
| $\mathrm{CH}_{3}$ | 3-M ethyltoluene | 1.1531 | 0.1250 | 0.1532 | 0.1057 | 0.1761 | 0.0600 | 1564.4 | 1594.5 |
| $\mathrm{CH}_{3}$ | 4-M ethyltoluene | 1.1391 | 0.1271 | 0.1538 | 0.0947 | 0.1768 | 0.0576 | 1568.2 | 1597.9 |
| $\mathrm{CH}_{3}$ | 2-Phenylpropene* | 1.2241 | 0.1312 | 0.1526 | 0.1115 | 0.1753 | 0.0597 | 1585.7 | 1613.4 |
| $\mathrm{CH}_{3}$ | 2-M ethylbutadiene* | 0.7960 | 0.1194 | 0.1478 | 0.1220 | 0.1687 | 0.0523 | 1585.7 | 1613.8 |
| C3 | Cyclohexene | 0.9593 | 0.1142 | 0.1481 | 0.0960 | 0.1685 | 0.0537 | 1617.1 | 1617.1 |
| C3 | Cyclooctene | 1.2958 | 0.1131 | 0.1476 | 0.0915 | 0.1686 | 0.0479 | 1585.7 | 1617.1 |
| C2 | M ethylenecyclobutane | 0.8212 | 0.1103 | 0.1467 | 0.1806 | 0.1675 | 0.0402 | 1585.7 | 1620.0 |
| C3 | 2-M ethylenenorbornene | 1.1833 | 0.1190 | 0.1476 | 0.1518 | 0.1675 | 0.0400 | 1599.5 | 1628.8 |
| C3 | 5-M ethylenenorbornene | 1.1257 | 0.1204 | 0.1495 | 0.1505 | 0.1688 | 0.0777 | 1602.9 | 1632.2 |
| $\mathrm{CH}_{3}$ | 2-M ethylpropene* | 0.7252 | 0.1086 | 0.1473 | 0.1727 | 0.1686 | 0.0380 | 1602.1 | 1633.0 |
| C4 | Bicyclo[3.2.1]octa-2-ene | 1.1951 | 0.1153 | 0.1486 | 0.1037 | 0.1683 | 0.0590 | 1603.7 | 1634.7 |
| C1 | 1-Phenylethene | 1.0857 | 0.1303 | 0.1526 | 0.0683 | 0.1754 | 0.0598 | 1604.1 | 1635.9 |
| C1 | Phenylcyclopropane | 1.2277 | 0.1278 | 0.1530 | 0.0661 | 0.1754 | 0.0597 | 1606.7 | 1639.3 |
| C1 | Vinylcyclopropane | 0.7866 | 0.1168 | 0.1465 | 0.0787 | 0.1667 | 0.0500 | 1617.1 | 1647.2 |
| C1 | $N$ aphthalene | 1.2165 | 0.1460 | 0.1598 | 0.0576 | 0.1814 | 0.0599 | 1605.8 | 1649.3 |
| C1 | Cyclobutene | 0.6245 | 0.1118 | 0.1479 | 0.1168 | 0.1683 | 0.0859 | 1627.6 | 1661.9 |
| C1 | Bicyclobutane* | 0.6287 | 0.1124 | 0.1456 | 0.1741 | 0.1601 | 0.0991 | 1635.9 | 1670.3 |
| C2 | N orbornadiene | 0.9380 | 0.1173 | 0.1509 | 0.1035 | 0.1699 | 0.0786 | 1637.2 | 1671.5 |
|  | Benzene* | 0.8003 | 0.1273 | 0.1517 | 0.0593 | 0.1744 | 0.0593 | 1635.5 | 1676.5 |
| C2 | N orbornene | 1.0219 | 0.1149 | 0.1492 | 0.1030 | 0.1680 | 0.0771 | 1648.1 | 1682.4 |
|  | Cyclohexane | 1.0065 | 0.1115 | 0.1282 | 0.0101 | 0.1461 | 0.0051 | 1665.2 | 1690.3 |
| C2 | Propene* | 0.5618 | 0.1056 | 0.1459 | 0.1291 | 0.1669 | 0.0487 | 1665.2 | 1697.9 |
| $\mathrm{CH}_{3}$ | 2,2-D imethylpropane* | 0.9351 | 0.1062 | 0.1244 | 0.1257 | 0.1429 | $-0.0068$ | 1673.6 | 1710.8 |
| $\mathrm{CH}_{3}$ | 3,3-D imethylbutene* | 1.0592 | 0.1082 | 0.1459 | 0.0956 | 0.1666 | 0.0467 |  | 1711.3 |
| $\mathrm{Cl}^{3}$ | M ethylcyclopropane* | 0.7079 | 0.1072 | 0.1349 | 0.1273 | 0.1521 | 0.0436 | 1679.5 | 1712.1 |
|  | Ethene* | 0.3811 | 0.1017 | 0.1438 | 0.0799 | 0.1649 | 0.0399 | 1677.8 | 1712.9 |

Table 2 (continued)

| A cidic $\mathrm{H}^{\text {a }}$ | M olecule | $\mathrm{V}_{\mathrm{mc}}$ | $\pi_{1}$ | $\varepsilon_{B}$ | q- | $\varepsilon_{\text {A }}$ | $\mathrm{q}_{+}$ | $\Delta_{\mathrm{a}} \mathrm{G} / \mathrm{kJ} \mathrm{mol}^{-1}$ | $\Delta_{\mathrm{a}} \mathrm{H} / \mathrm{kJ} \mathrm{mol}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C1 | Bicyclopentane* | 0.7866 | 0.1111 | 0.1289 | 0.0936 | 0.1467 | 0.0677 | 1719.6 | 1719.6 |
| $\mathrm{CH}_{3}$ | But-1-ene* | 0.7275 | 0.1075 | 0.1459 | 0.1165 | 0.1667 | 0.0490 | 1690.3 | 1723.8 |
| C2 | 2-M ethylpropane* | 0.7787 | 0.1040 | 0.1244 | 0.0823 | 0.1442 | 0.0130 | 1691.2 | 1727.6 |
| C2 | Propane* | 0.6412 | 0.0974 | 0.1222 | 0.0346 | 0.1430 | 0.0046 | 1703.3 | 1738.9 |
| C2 | Butane* | 0.8215 | 0.0989 | 0.1235 | 0.0203 | 0.1440 | 0.0043 | 1703.3 | 1739.3 |
|  | Cyclopentane* | 0.8609 | 0.1062 | 0.1250 | 0.0165 | 0.1462 | 0.0082 | 1704.1 | 1741.0 |
|  | M ethane* | 0.2715 | 0.0904 | 0.1069 | -0.0704 | 0.1342 | -0.0176 | 1709.6 | 1743.5 |
|  | Cyclopropane* | 0.5203 | 0.1084 | 0.1313 | 0.0736 | 0.1502 | 0.0368 | 1707.9 | 1744.7 |
|  | Cyclobutane* | 0.7089 | 0.1033 | 0.1275 | 0.0336 | 0.1452 | 0.0168 | 1708.7 | 1746.4 |
|  | Ethane* | 0.4391 | 0.0994 | 0.1186 | -0.0166 | 0.1405 | -0.0055 | 1720.9 | 1757.7 |
| The following compounds have no empirical values or are outliers. Outliers have empirical values listed |  |  |  |  |  |  |  |  |  |
| $\mathrm{CH}_{3}$ | But-2-ene | 0.7232 | 0.1113 | 0.1479 | 0.1028 | 0.1686 | 0.0486 |  |  |
|  | Cubane | 0.9431 | 0.1252 | 0.1361 | 0.0661 | 0.1460 | 0.0661 |  |  |
| C3 | Cycloocta-1,4-diene | 1.1933 | 0.1198 | 0.1524 | 0.1073 | 0.1721 | 0.0550 |  |  |
| C3 | Cyclopentadiene* | 0.7321 | 0.1147 | 0.1552 | 0.1182 | 0.1750 | 0.0726 | 1454.8 | 1480.7 |
|  | D initramide | 0.5490 | 0.1450 | 0.1178 | 0.4055 | 0.1994 | 0.2688 | 1242.6 |  |
| $\mathrm{CH}_{3}$ | 2-M ethyltoluene | 1.1800 | 0.1217 | 0.1533 | 0.0809 | 0.1762 | 0.0603 |  |  |
|  | $\mathrm{NH}_{3}{ }^{*}$ | 0.2199 | 0.0847 | 0.1337 | 0.2268 | 0.1347 | 0.0756 | 1657.3 |  |
| C1 | $N$ itrocubane | 1.1531 | 0.1272 | 0.1321 | 0.3358 | 0.1804 | 0.0912 |  |  |
|  | N itramine | 0.3699 | 0.1267 | 0.1261 | 0.3249 | 0.1839 | 0.1625 |  |  |
| C1 | 1-N itropropane | 0.7867 | 0.1145 | 0.1310 | 0.3357 | 0.1807 | 0.0551 |  | 1688.7 |
| $\mathrm{CH}_{3}$ | 2-N itropropane | 0.6998 | 0.1246 | 0.1368 | 0.3414 | 0.1810 | 0.0746 |  |  |
|  | Trinitromethane | 0.7720 | 0.1494 | 0.1154 | 0.2695 | 0.2018 | 0.1593 |  |  |
|  | Triphenylcyclopropene | 2.5265 | 0.1601 | 0.1616 | 0.0791 | 0.1851 | 0.0643 | 1577.4 | 1612.9 |

${ }^{\text {a }}$ A cidic H , the number of the carbon or type of group $\left(\mathrm{CH}_{3}\right)$ to which the acidic hydrogen is attached; numbering is based on IUPAC protocol. See Fig. 1 for some complex structures. A ssignments are from the $N$ egion database, original references, calculations on isomers and/or consultation with organic chemistry colleagues. Experimental results do not necessarily provide knowledge of the acidic site. N othing is written when there is no acid site ambiguity.

In turn, the free energy is linearly related to an energy term such as enthalpy.

The TLSER descriptors are summarized in Table 1; they apply to a neutral molecular model. $\mathrm{V}_{\text {mo }}$, the molecular volume, can model the size of a cavity for placing the solute in a solvent and/or can be related to dispersive interactions. The polarizability index, $\pi_{1}$, models the polarizability and may berelated to dispersive interactions. The $\varepsilon_{\mathrm{B}}$ and $\varepsilon_{\mathrm{A}}$ terms model the covalent hydrogen bond acceptor basicity (HBAB) and hydrogen bond donor activity (HBDA), respectively; while the $q_{-}$and $q_{+}$terms model electrostatic HBB and HBA, also respectively. The $\varepsilon_{\mathbf{B}}$ and $\varepsilon_{\mathrm{A}}$ use linear functions of the highest occupied molecular orbital (HOM O) energy and the lowest unoccupied molecular orbital (LUMO) energy, respectively. The electrostatic HBB descriptor is the largest negative atomic formal charge, $q_{-}$; the corresponding HBA descriptor is the formal charge, $\mathrm{q}_{+}$, on the most positive H atom.

In this application the LUMO (and electron affinity) and HOMO (and ionization potential) are assumed to be vertical quantities in the sense of the Franck-Condon principle; however, this is not always the case for the LUM O. An added electron does not necessarily attach to the molecule to form a bound anion; the added electron may remain free The LUM O and HOMO are used here as models; by their very nature models do not completely represent the real system.

Eqn. (2) can be used in two ways; it can predict values and serve as a molecular probe For prediction, the molecular parameters are calculated for a compound and substituted into the equation. A s a probe, the physical meaning of a statistically significant parameter can suggest something about the process associated with the property. For example, if the hydrogen bonding activity, $\varepsilon_{\mathrm{A}}$ or $\mathrm{q}_{+}$, is significant for some biological property then a receptor site might have a hydrogen bond basicity function. Their coefficients, e or $f$, could beinterpreted as a measure of the hydrogen bond basicity of the receptor site.
This paper calculates $\Delta_{\mathrm{a}} \mathrm{H}(\mathrm{RH})$ values with direct methods, which have a good theoretical basis, and with the TLSER correlation equation in order to explore, further, the applicability of the TLSER descriptors for calculating properties for ener-
getic materials. A previous study of energetic compounds (including trinitrotoluene) examined the correlation of HPLC (high performance liquid chromatography) capacity factors with TLSER parameters. ${ }^{16} \mathrm{~A}$ statistically significant and physically reasonable equation can suggest using TLSER descriptors in relationships for other properties.
An earlier, related paper ${ }^{12}$ examined correlations for gas phase acidities of some carboxylic acids, alcohols, silanols, anilines and a small number of hydrocarbons. For the hydrocarbons the measured quantity was the activation energy for the process in eqn. (1). This paper uses a much larger set of hydrocarbons (and related nitro derivatives). Because of the need for an adequate statistical sample size, this study focuses on hydrocarbons and nitrohydrocarbons. A zides, for example, are not included.

## Procedure

The M NDO, A M 1 and PM 3 protocols in M OPAC 6 were used to get the semiempirical theoretical $\Delta \mathrm{H}_{\mathrm{a}}$ values for 37 molecules (marked with * in Table 2). The heats of formation of the anion and molecule were taken from the M OPAC output while the heat formation of the hydrogen ion was taken as the empirical value, $1530 \mathrm{~kJ} \mathrm{~mol}^{-1} .{ }^{15}$ The model for the radical anions was kept simple; Jahn-Teller distortions due to degeneracy (such as with methane) were ignored and their (often) unbound nature was not considered as relevant. GAU SSIA N 92 was used to calculate the $6-31+G$ values for those compounds not found in the literature

D ata for the compounds listed in Table 2 were taken from the 19A and 19B NIST Positive and N egative Ion Energetics D atabase. ${ }^{1}$ The compound set was selected to provide a reasonable number of small hydrocarbons and nitro group containing derivatives. In addition, some compounds for which there were no empirical data were included so that their values could be calculated. $\Delta_{\mathrm{a}} \mathrm{H}$ (rather than $\Delta_{\mathrm{a}} \mathrm{G}$ ) values were used in the correlations since the semiempirical calculations yield $\Delta_{f} \mathrm{H}$ values directly. In fact, the semiempirical methods are parameterized based on heats of formation. In converting to kJ from kcal one

biclo 2.1 ]cta-2,
Fig. 1 Representative compound structures with position indicators
more digit was retained than was significant so as to minimize error. Not all data were of the same uncertainty; many uncertainties are around $\pm 8 \mathrm{~kJ} \mathrm{~mol}^{-1}$ while some were $\pm 20 \mathrm{~kJ}$ $\mathrm{mol}^{-1}$ or higher.

When data for more than one H atom on a molecule were available, often the site with the lowest $\Delta_{\mathrm{a}} \mathrm{H}$ value was chosen. In the case of phenylethane, for example, the database indicates that the $\mathrm{PhCH}_{2} \mathrm{CH}_{2}{ }^{-}$ion involves ca. $110 \mathrm{~kJ} \mathrm{~mol}^{-1}$ more energy than the $\mathrm{PhCH}^{-} \mathrm{CH}_{3}$ ion. Fig. 1 contains some structures to help identify compounds; position numbers, based on IU PAC protocol, are provided to help locate acidic sites. Experiment, particularly ion cyclotron resonance (ICR), does not necessarily identify the acidic site; ${ }^{17}$ however, the apparent acidic sites (as gathered from theN egion D atabase, original references, some isomer calculations and consultation with organic chemistry colleagues) are indicated before the name in Table 2. When there is only one site possible nothing is written. From the standpoint of these calculations it was only necessary to identify the acidic sites for the compounds in Table 4

The molecular geometry description (Z-matrix) was modelled and viewed using PCM ODEL (Serena Software, Bloomington, IN 47402-3076) and MMADS (in house program). ${ }^{18}$ The Hamiltonian was modelled with the M NDO, AM 1 and PM 3 algorithms in M OPAC6 (QCPE); the output gave the optimized geometry, energies, polarizabilities and Coulson formal charges and heats of formation. The M OPAC calculations were done with keywords, EF and PRECISE. The TLSER molecular parameters were taken from the MNDO results; they were extracted from the M OPAC files with M AD CAP (in house program). ${ }^{19}$

The equation parameters were obtained by multilinear correlation (regression) analysis. The quality of the correlation equations was judged by the statistical parameters. Guidelines for acceptance were: correlation coefficient, R, near 0.90 or higher (variance, $R^{2}>0.80$ ); terms significant at the 0.95 leve or higher [ $\mathrm{P}(2$-tail $)<0.05$ ], and low variable collinearity [variance inflation factor (VIF) < 5]. While it is stated that VIF values less than 10 are statistically satisfactory, we chose the more stringent criterion. When there was too much crosscorrelation the parameter with the least (lowest t-stat) significance was eliminated. Outliers were compounds with Student deleted residuals greater than three.

## Results

Table 4 contains some selected values calculated directly by TLSER [eqn. (7) in Table 6], M N D O, A M 1, PM 3 and ab initio values from R itchie and Bacharach ${ }^{1}$ as well as GAUSSIAN 92
calculated values done for this study. Table 6 contains the TLSER correlation equations along with the statistical parameters. Table 5 contains eqns. (3-6) which refer to correlations of the experimental values against ab initio ( $6-31+G)$, MNDO, AM 1 and PM 3 calculated $\Delta_{\mathrm{a}} \mathrm{H}$ values, respectively. Correlations on the hydrocarbons alone and the nitro compounds alone were done but not recorded here. The equations accounted for considerably less than $80 \%$ of the variance. Table 3 contains TLSER parameters for the compounds; these are arranged in ascending (decreasing acidity) order of experimental $\Delta_{\mathrm{a}} \mathrm{H}$ values (where known). One more significant figure than is justified is retained since most empirical values are given to the nearest $0.1 \mathrm{kcal} \mathrm{mol}^{-1}$ and several compounds are very close in value. Table 4 contains the TLSER calculated $\Delta_{\mathrm{a}} \mathrm{H}$ values along with residuals where empirical values are known.

## D iscussion

Examination of Table 4 shows that empirical and directly calculated values do not agree as well as one would like; in fact, the $6-31+G$ ab initio values tend to be higher than empirical values. Consequently, correlation equations between the empirical and theoretical values were obtained in order to improve the fit. These appear as eqns. (3-6) in Table 5, and are repeated
$\Delta_{\mathrm{a}} \mathrm{H}($ calc $)=297.26 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.78358 \Delta_{\mathrm{a}} \mathrm{H}($ ab initio $)$
$\Delta_{\mathrm{a}} \mathrm{H}($ calc $)=518.13 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.67691 \Delta_{\mathrm{a}} \mathrm{H}\left(\mathrm{MNDO}^{2}\right)$
$\Delta_{\mathrm{a}} \mathrm{H}($ calc $)=557.19 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.64892 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{AM} 1)$
$\Delta_{\mathrm{a}} \mathrm{H}($ calc $)=374.62 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.77104 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{PM} 3)$
here without the statistical parameters. At this point it is hel pful to recall that theoretically calculated results often are more useful for examining relative trends rather than getting absolute values. This is particularly appropriate here since the heats of formation of the molecule and ion are used to calculate $\Delta_{\mathrm{a}} \mathrm{H}$. While semiempirical methods have been parameterized using empirical heats of formation, $\Delta_{\mathrm{f}} \mathrm{H}$, calculated $\Delta_{\mathrm{f}} \mathrm{H}$ values do not always agree with experiment. That may contribute to the scatter in Table 4 and the variance in the equations of Table 6. [For that matter, the $6-31+\mathrm{G}$ level ab initio values seem to have as much scatter as the semiempirical ones; most are higher than the empirical values. H owever, eqns (3-6) show that these $6-31+G$ values correlate better with the empirical value]
A possible contribution to the lack of empirical and theoretical agreement could be in the $\Delta_{f} H\left(\mathrm{R}^{-}\right)$calculations; the exact location for the acidic hydrogen was not always evident from the experimental information. While there are consistent trends for these directly calculated values, Table 6 shows the M ND O regression fit, eqn. (4), of empirical $\Delta_{\mathrm{a}} \mathrm{H}$ values with the calculated values had a variance $\left(\mathrm{R}^{2}\right)$ of 0.56 and a standard deviation of $74 \mathrm{~kJ} \mathrm{~mol}^{-1}$ (when cyclopentadiene is retained). This should be compared with the early calculation of electron affinities by Dewar and R zepa ${ }^{20}$ which gave a standard deviation of $41 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and exhibited systematic errors for different classes of molecules. The A M 1 and PM 3 eqns. (5) and (6), give better fits but still with variances less than 0.80 when the outliers are retained.

Hartree-Fock level ab initio techniques do not improve this situation. The methane values calculated with different basis sets by Ritchie and Bacharach ${ }^{1}$ are all higher then empirical observation just as in other direct value cases. A calculation on another small molecule, ammonia, with the $6-31+\mathrm{G}$ basis set corresponding to the Ritchie calculations also gives a much larger value of the acidity compared to experiment. Similarly, Koppel et al. ${ }^{21}$ performed calculations on 14 very strong neutral CH acids using the 3 -21G basis set. The calculated values of $\Delta_{\mathrm{a}} \mathrm{G}$ were systematically larger than the experimental values.

Table 3 Compounds with TLSER calculated $\Delta_{\mathrm{a}} \mathrm{H}$ values and residuals $\left(\mathrm{kJ} \mathrm{mol}{ }^{-1}\right)^{\text {a }}$

| M olecule | Calculated | Residual | Stud. resid. ${ }^{\text {b }}$ | Empirical | M olecule | Calculated | Residual | Stud. resid. ${ }^{\text {b }}$ | Empirical |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| N itric acid | 1391.7 | -34.0 | -0.96 | 1357.7 | Benzene | 1562.0 | 22.5 | 0.55 | 1584.5 |
| Fluoradene | 1461.7 | -70.1 | -1.77 | 1391.6 | 2-Phenylpropane | 1565.3 | 20.5 | 0.50 | 1585.7 |
| 1,3-D iphenylindene | 1424.1 | -21.2 | -0.54 | 1402.9 | Bicyclo[3.2.1]octa-2,6- | 1600.0 | -11.8 | -0.29 | 1588.2 |
| 1,2,3-Triphenylindene | 1363.3 | 40.8 | 1.11 | 1404.2 | diene |  |  |  |  |
| 2-Phenyl-5-p- | 1462.9 | -50.3 | -1.27 | 1412.5 | Ethylbenzene | 1577.4 | 11.7 | 0.29 | 1589.1 |
| tolylcyclopentadiene |  |  |  |  | Pentyne | 1591.5 | -2.4 | -0.06 | 1589.1 |
| 2,5-D iphenyl- | 1479.4 | -66.5 | -1.67 | 1412.9 | Propadiene | 1676.3 | -83.8 | -2.1 | 1592.4 |
| cyclopentadiene |  |  |  |  | Toluene | 1597.9 | -4.6 | -0.11 | 1593.3 |
| $N$ itrous acid | 1457.0 | -33.2 | -0.89 | 1423.8 | Propyne | 1628.9 | -34.4 | -0.89 | 1594.5 |
| 9 -Phenylfluorene | 1447.4 | -11.0 | -0.27 | 1436.4 | 3-M ethyltoluene | 1578.0 | 16.5 | 0.40 | 1594.5 |
| 9-N eopentylfluorene | 1443.3 | 8.5 | 0.21 | 1451.8 | 4-M ethyltoluene | 1579.3 | 18.6 | 0.45 | 1597.9 |
| 9-I sobutylfluorene | 1455.7 | 12.0 | 0.30 | 1467.7 | 2-Phenylpropane | 1573.5 | 39.9 | 0.98 | 1613.4 |
| 9-M ethylfluorene | 1513.3 | -45.1 | -1.11 | 1468.2 | 2-M ethylbutadiene | 1641.4 | -27.6 | -0.68 | 1613.8 |
| 9-tert-Butylfluorene | 1453.4 | 15.2 | 0.38 | 1468.6 | Cyclohexene | 1626.5 | -9.3 | -0.23 | 1617.1 |
| 9-EthyIfluorene | 1491.1 | -21.7 | -0.53 | 1469.4 | Cyclooctene | 1593.7 | 23.4 | 0.57 | 1617.1 |
| 9-I sopropylfluorene | 1476.1 | -6.3 | -0.16 | 1469.8 | M ethylenecyclobutane | 1649.3 | -29.2 | -0.72 | 1620.0 |
| Fluorene | 1525.9 | -54.0 | -1.34 | 1471.9 | 2-M ethylenenorbornene | 1615.9 | 13.0 | 0.32 | 1628.8 |
| Indene | 1571.5 | -98.8 | -2.52 | 1472.8 | 5-M ethylenenorbornene | 1598.1 | 34.1 | 0.83 | 1632.2 |
| 4-N itrotoluene | 1466.5 | 8.4 | 0.21 | 1474.9 | 2-M ethylpropene | 1656.6 | -23.6 | -0.58 | 1633.0 |
| 2-M ethylfluorene | 1501.8 | -26.5 | -0.65 | 1475.3 | Bicyclo[3.2.1]octa-2-ene | 1601.7 | 33.0 | 0.81 | 1634.7 |
| 6,6-D imethylfulvene | 1531.1 | -49.6 | -1.23 | 1481.6 | Phenylethene | 1586.8 | 49.2 | 1.21 | 1635.9 |
| $N$ itrobenzene | 1490.2 | -8.2 | -0.20 | 1482.0 | Phenylcyclopropane | 1573.9 | 65.4 | 1.62 | 1639.3 |
| N itro-2,2- | 1485.2 | 1.0 | 0.025 | 1486.2 | Vinylcyclopropane | 1650.8 | -3.5 | -0.09 | 1647.2 |
| dimethylpropane |  |  |  |  | $N$ aphthalene | 1565.2 | 84.1 | 2.13 | 1649.3 |
| $N$ itroethane | 1531.1 | -41.5 | -1.06 | 1489.5 | Cyclobutene | 1641.6 | 20.3 | 0.50 | 1661.9 |
| $N$ itroethyne | 1416.1 | 73.4 | 1.97 | 1489.5 | Bicyclobutane | 1670.5 | -0.2 | -0.01 | 1670.3 |
| 2-N itropropane | 1516.8 | -26.8 | -0.68 | 1489.9 | N orbornadiene | 1615.7 | 55.8 | 1.38 | 1671.5 |
| 2-N itrotoluene | 1478.8 | 11.2 | 0.28 | 1489.9 | Benzene | 1618.6 | 57.9 | 1.44 | 1676.5 |
| N itromethane | 1544.6 | -53.4 | -1.39 | 1491.2 | N orbornene | 1612.5 | 69.9 | 1.74 | 1682.4 |
| Triphenylmethane | 1456.6 | 44.2 | 1.12 | 1500.8 | Cyclohexane | 1706.5 | -16.2 | -0.41 | 1690.3 |
| Pentamethyl- | 1560.8 | -51.2 | -1.27 | 1509.6 | Propene | 1671.5 | 26.3 | 0.65 | 1697.9 |
| cyclopentadiene |  |  |  |  | 2,2-D imethylpropane | 1725.6 | -14.7 | -0.37 | 1710.8 |
| $N$ itroethene | 1461.7 | 52.9 | 1.37 | 1514.6 | 3,3-D imethylbutene | 1623.8 | 87.5 | 2.19 | 1711.3 |
| 9-M ethylanthracene | 1491.4 | 24.1 | 0.60 | 1515.4 | M ethylcyclopropane | 1703.8 | 8.3 | 0.20 | 1712.1 |
| 3 -N itrotoluene | 1479.4 | 39.0 | 0.97 | 1518.4 | Ethene | 1698.8 | 14.2 | 0.35 | 1712.9 |
| D iphenylmethane | 1520.2 | 1.1 | 0.028 | 1521.3 | Bicyclopentane | 1689.9 | 29.7 | 0.75 | 1719.6 |
| N itrocyclopropane | 1499.2 | 35.1 | 0.88 | 1534.3 | But-1-ene | 1655.3 | 68.5 | 1.71 | 1723.8 |
| 1-Phenylprop-2-ene | 1570.6 | -30.5 | -0.74 | 1504.1 | 2-M ethylpropane | 1722.3 | 5.3 | 0.13 | 1727.6 |
| 1,4-Penta-1,4-diene | 1641.8 | -97.1 | -2.46 | 1544.7 | Propane | 1740.8 | -1.9 | -0.05 | 1738.9 |
| Phenylethyne | 1527.8 | 23.2 | 0.59 | 1551.0 | Butane | 1721.1 | 18.2 | 0.46 | 1739.3 |
| Cyclohexa-1,3-diene | 1615.5 | -53.6 | -1.34 | 1561.9 | Cyclopentane | 1708.1 | 32.9 | 0.83 | 1741.0 |
| 1-M ethylnaphthalene | 1549.1 | 16.1 | 0.40 | 1565.2 | M ethane | 1787.3 | -43.8 | -1.17 | 1743.5 |
| Cycloheptatriene | 1585.3 | -15.5 | -0.38 | 1569.8 | Cyclopropane | 1724.6 | 20.1 | 0.50 | 1744.7 |
| Cycloocta-1,3-diene | 1588.0 | -11.9 | -0.29 | 1576.1 | Cyclobutane | 1732.7 | 13.7 | 0.34 | 1746.4 |
| 3,3-D imethylbutyne | 1581.8 | -0.3 | -0.01 | 1581.6 | Ethane | 1768.5 | -10.8 | -0.28 | 1757.7 |
| Ethyne | 1651.4 | -69.8 | -1.84 | 1581.6 |  |  |  |  |  |
| The following compounds have no empirical values or are outliers. |  |  |  |  |  |  |  |  |  |
| But-2-ene | 1652.3 |  |  |  | N itrocubane | 1462.1 |  |  |  |
| Cubane | 1704.1 |  |  |  | N itramine | 1458.3 |  |  |  |
| Cycloocta-1,4-diene | 1596.6 |  |  |  | N itropropane | 1515.8 |  |  |  |
| Cyclopentadiene | 1626.5 | -145.8 | -3.54 | 1480.7 | $N$ itropropene | 1531.3 |  |  |  |
| D initramide | 1260.5 |  |  |  | Trinitromethane | 1282.5 |  |  |  |
| 2-M ethyltoluene | 1575.1 |  |  |  | Triphenylcyclopropene | 1414.7 | 198.2 | 4.81 | 1612.9 |
| $\mathrm{NH}_{3}$ | 1826.6 | -137.9 | -3.35 | 1688.7 |  |  |  |  |  |

${ }^{\text {a }}$ See Table 2 for suggested acidic sites. ${ }^{\text {b }}$ Student(ized) deleted residual error.

They got a straight line regression, $\Delta_{\mathrm{a}} \mathrm{G}($ calc $)=208 \mathrm{~kJ}$ $\mathrm{mol}^{-1}+0.811 \Delta_{\mathrm{a}} \mathrm{G}(3-21 \mathrm{G})$. A simple regression of ab initio values in Table 3 calculated with $6-31+G$ basis set is written as eqn. (3) in Table 5. To produce ab initio results that are in close agreement with experiment it is necessary to use very high levels of theory. Smith and Radom ${ }^{22}$ obtained gas phase acidity values for 23 small molecules using G2 theory with a mean error of $6 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and consistently within $10 \mathrm{~kJ} \mathrm{~mol}^{-1}$. In an earlier study of proton affinities, DeF rees and McL ean ${ }^{23}$ obtained results within $8 \mathrm{~kJ} \mathrm{~mol}^{-1}$ using $\mathrm{M} \mathrm{P} 4 / 6-311++\mathrm{G}$ (3df,3pd) for small neutral molecules and ions.

Examination of eqn. (7) for the TLSER descriptors shows

$$
\begin{align*}
\Delta_{\mathrm{a}} \mathrm{H} & = \\
& -101.9 \mathrm{~V}_{\mathrm{mc}}+3471 \varepsilon_{\mathbf{B}}-5568 \varepsilon_{\mathbf{A}}-606.3 \mathrm{q}_{+}+2181 \tag{7}
\end{align*}
$$

that the correlation is physically reasonable and statistically acceptable. The physically reasonable nature is indicated by the way $\Delta_{\mathrm{a}} \mathrm{H}$ and $\Delta_{\mathrm{a}} \mathrm{G}$ decrease (indicating increase in acidity) with increasing acidity parameters, $\varepsilon_{\mathrm{A}}$ and $\mathrm{q}_{+}$. Furthermore, they increase (indicating decrease in acidity) with increasing basicity parameter, $\varepsilon_{\mathrm{B}}$. The decrease of $\Delta_{\mathrm{a}} \mathrm{H}$ and $\Delta_{\mathrm{a}} \mathrm{G}$ with $\mathrm{V}_{\mathrm{mc}}$ is reasonable since a hydrogen atom can be more readily removed from a large molecule; less perturbation in structure is involved.

The statistically reasonable nature of eqn. (7) is indicated as follows. The correlation coefficient values, R, show that they account for more than $80 \%$ of the variance The coefficients are all significant above the 0.000 level. Furthermore, VIF values indicate that the descriptors are within the acceptable range for orthogonality. The SD values are about double the largest experimental uncertainty of $\mathrm{ca} . \pm 21 \mathrm{~kJ} \mathrm{~mol}^{-1}$; this indicates

Table $4 \quad \Delta_{\mathrm{a}} \mathrm{H}\left(\mathrm{kJ} \mathrm{mol}^{-1}\right)$ values for selected compounds by various methods ${ }^{\text {a }}$

| M olecule | Experiment | TLSER ${ }^{\text {b }}$ | M NDO | AM 1 | PM 3 | $6-31+\mathrm{G}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Ethane | 1757.7 | 1768.5 | 1727.0 | 1747.2 | 1738.4 | 1835.7 |
| Cyclopropane | 1744.7 | 1724.6 | 1721.4 | 1739.7 | 1714.0 | 1819.0 |
| M ethane | 1743.5 | 1787.3 | 1817.8 | 1808.2 | 1800.0 | 1813.5 |
| Bicyclopentane | 1719.6 | 1689.9 | 1741.8 | 1729.5 | 1688.6 | 1805.4 |
| M ethylcyclopropane | 1712.1 | 1703.8 | 1645.0 | 1702.5 | 1679.2 | 1813.3 |
| Ethene | 1712.9 | 1698.8 | 1763.1 | 1746.0 | 1718.6 | 1770.3 |
| Benzene | 1676.5 | 1618.6 | 1696.10 | 1679.5 | 1648.1 | 1743.8 |
| Bicyclobutane | 1670.3 | 1670.5 | 1714.2 | 1701.6 | 1659.0 | 1744.1 |
| Toluene | 1593.1 | 1597.9 | 1550.5 | 1556.6 | 1548.5 | 1680.1 |
| Ethyne | 1581.6 | 1651.4 | 1726.0 | 1674.8 | 1637.4 | 1610.3 |
| 3-N itrotoluene | 1518.4 | 1479.4 | 1565.2 | 1579.8 | 1540.9 | 1636.7 |
| N itromethane | 1491.2 | 1544.6 | 1453.7 | 1449.4 | 1415.3 | 1471.8 |
| 2-N itropropane | 1489.9 | 1516.8 | unstable | unstable | unstable | 1480.3 |
| 2-N itrotoluene | 1489.9 | 1478.8 | 1446.2 | 1441.8 | 1431.7 | 1520.8 |
| 4-N itrotoluene | 1489.9 | 1466.5 | 1422.8 | 1426.5 | 1415.3 | 1506.3 |
| N itroethane | 1489.5 | 1531.1 | 1422.6 | 1380.7 | 1397.0 | 1474.2 |
| Nitrobenzene | 1482.0 | 1490.2 | 1605.9 | 1579.1 | 1572.5 | 1640.8 |
| Cubane | unad |  | 1739.9 | 1720.6 | 1687.0 | 1803.7 |
| Nitrocubane | una |  | 1666.0 | 1644.0 | 1619.3 | 1682.3 |

${ }^{a}$ See Table 2 for acidic sites. ${ }^{\text {b }}$ TLSER values calculated with eqn. (7), Table 6. ${ }^{\mathrm{c}} \mathrm{A}$ nion calculations resulted in fragmentation. ${ }^{\text {d }}$ una, empirical value unavailable.

Table 5 Correlation equations for $\Delta_{\mathrm{a}} \mathrm{H}$ (empirical) vs. $\Delta_{\mathrm{a}} \mathrm{H}$ (theory)

| Equation | N | R | SD | F |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\Delta_{\mathrm{a}} \mathrm{H}(\mathrm{calc})=297.26 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.78358 \Delta_{\mathrm{a}} \mathrm{H}($ ab initio $)$ | $18^{\text {a }}$ | 0.936 | 40.5 | 112 | (3) |
| Outlier: nitrobenzene retained |  |  |  |  |  |
| $\Delta_{\mathrm{a}} \mathrm{H}($ calc $)=318.45 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.77444 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{ab}$ initio) | 17 | 0.960 | 32.0 | 175 | (3a) |
| Outlier: nitrobenzene removed |  |  |  |  |  |
| $\Delta_{\mathrm{a}} \mathrm{H}(\mathrm{calc})=518.13 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.67691 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{MNDO})$ | $37^{\text {b }}$ | 0.750 | 73.6 | 45.0 | (4) |
| Outlier: cyclopentadiene retained |  |  |  |  |  |
| $\Delta_{\mathrm{a}} \mathrm{H}(\mathrm{calc})=456.94 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.71808 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{MNDO})$ | 36 | 0.807 | 65.1 | 63.4 | (4a) |
| Outlier: cyclopentadiene removed |  |  |  |  |  |
| $\Delta_{\mathrm{a}} \mathrm{H}($ calc $)=557.19 \mathrm{~kJ} \mathrm{~mol}{ }^{-1}+0.64892 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{AM} \mathrm{1)}$ | $37^{\text {b }}$ | 0.774 | 70.4 | 52.5 | (5) |
| Outlier: nitrobenzene retained |  |  |  |  |  |
| $\Delta_{\mathrm{a}} \mathrm{H}(\mathrm{calc})=431.06 \mathrm{~kJ} \mathrm{~mol}^{-1}+73571 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{AM} \mathrm{1)}$ | 34 | 0.913 | 44.5 | 161 | (5a) |
| Outlier: nitrobenzene, cyclopentadiene, 3 -phenylpropene removed |  |  |  |  |  |
| $\Delta_{\mathrm{a}} \mathrm{H}($ calc $)=374.62 \mathrm{~kJ} \mathrm{~mol}^{-1}+0.77104 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{PM} \mathrm{3)}$ | $37^{\text {b }}$ | 0.838 | 60.7 | 82.6 | (6) |
| Outlier: cyclopentadiene retained |  |  |  |  |  |
| $\Delta_{\mathrm{a}} \mathrm{H}($ calc $)=342.08 \mathrm{~kJ} \mathrm{~mol}^{-1^{\prime}}+0.79441 \Delta_{\mathrm{a}} \mathrm{H}(\mathrm{PM} 3)$ | 36 | 0.881 | 52.1 | 118 | (6a) |
| Outlier: cyclopentadiene removed |  |  |  |  |  |

${ }^{\text {a }}$ See Table 4 for list of compounds. ${ }^{\text {b }}$ See Table 2 for list of compounds, those with *.

Table 6 Correlation equation for $\Delta_{\mathrm{a}} \mathrm{H}$ and $\Delta_{\mathrm{a}} G\left(\mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ vs. TLSER descriptors

| $\Delta_{\mathrm{a}} \mathrm{H}=$ | $-101.9 \mathrm{~V}_{\mathbf{m c}}$ | $+3471 \varepsilon_{\mathbf{B}}$ | $-5568 \varepsilon_{\mathbf{A}}$ | $-606.3 \mathrm{q}_{+}+2181$ | (7) |
| :--- | :---: | :---: | :---: | :---: | :--- | :--- |
| $\pm$ | 10.6 | 573 | 525 | 126.9 | 76 |
| t-stat | 9.58 | 6.05 | 10.6 | 4.78 | 28.9 |
| P(2-tail) | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| VIF | 2.00 | 2.64 | 2.39 | 1.49 |  |
|  | $\mathrm{~N}=86$ | $\mathrm{R}=0.920$ | $\mathrm{SD}=41.2$ | $\mathrm{~F}=112$ |  |

Outliers: triphenylcyclopropene, cyclopentadiene, $\mathrm{NH}_{3}$ dropped.

| $\Delta_{\mathrm{a}} \mathrm{G}=$ | $-101.4 \mathrm{~V}_{\mathbf{m c}}$ | $+3391 \varepsilon_{\mathbf{B}}$ | $-5316 \varepsilon_{\mathbf{A}}$ | -616.0 | $\mathrm{q}_{+}$ | +2117 |
| :--- | :---: | :---: | :---: | :---: | :--- | :--- |
| $\pm$ | 10.0 | 510 | 494 | 116.2 | 73 |  |
| (7a) |  |  |  |  |  |  |
| t-stat | 10.1 | 6.65 | 10.8 | 5.30 | 28.9 |  |
| P(2-tail) | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |  |
| VIF | 2.04 | 2.48 | 2.40 | 1.83 |  |  |
|  | $\mathrm{~N}=85$ | $\mathrm{R}=0.933$ | $\mathrm{SD}=38.9$ | $\mathrm{~F}=133$ |  |  |

Outliers: triphenylcyclopropene, cyclopentadiene, $\mathrm{NH}_{3}$ dropped.
that the equation is not an artifact. A Iso, the SD value repre sents about $10 \%$ of the range of $\Delta_{\mathrm{a}} \mathrm{H}$ and $\Delta_{\mathrm{a}} \mathrm{G}$ values.

Eqn. (7) is in essential agreement with correlations in an earl-
ier paper on gas phase acidity. ${ }^{12}$ With only eight small hydrocarbons, $\varepsilon_{\mathrm{A}}$ [with negative sign as in eqn. (7)] was the only significant parameter for $\Delta_{\mathrm{a}} \mathrm{H}, \mathrm{R}$ was 0.823 with SD being 25 . For 16 hydrocarbons, the activation energy for deuterium exchange, expected to be related to $\Delta_{\mathrm{a}} \mathrm{H}, \varepsilon_{\mathbf{B}}$ (with positive sign) was the only significant parameter; R was 0.955 and SD was 9.6.

Comparison of calculated and empirical values in Table 3 gives an idea of the ability of TLSER to reproduce $\Delta_{\mathrm{a}} \mathrm{H}$ values. The SD value, $\pm 41 \mathrm{~kJ} \mathrm{~mol}^{-1}$, for eqn. (7), is from five to two times the empirical uncertainties, 8 to $21 \mathrm{~kJ} \mathrm{~mol}^{-1}$; hence, the ordering of the TLSER gas phase acidities would not be expected to be highly consistent with the empirical order. This would be especially true for compounds with close empirical gas phase acidities. However, there are some groups that do follow the empirical trends fairly well. The TLSER predicted $\Delta_{\mathrm{a}} \mathrm{H}$ order for nitroalkanes is-nitro-2,2-dimethylpropane < 2nitropropane < nitroethane < nitromethane. This essentially agrees with the empirical order-nitro-2,2-dimethylpropane < nitroethane < nitropropane < nitromethane-when noting that the empirical values for nitropropane and nitroethane are very close. Similarly, the relative $\Delta_{\mathrm{a}} \mathrm{H}$ order for a group of aromatics matches experiment-4-nitrotoluene $<2$ nitrotoluene $<3$-nitrotoluene $<$ toluene $<$ benzene. A nother
sequence-9-methylanthracene < 1-methylnaphthalene < the 3 - and 4-methyltoluenes < benzene-matches experiment, also. However, the empirical sequence-toluene < 3-methyltoluene < 4-methyltoluene (2-methyltoluene value not available)-is not matched in the TLSER calculations. The TLSER sequence places toluene last-2-methyl- < 3-methyl-<4-methyl- < toluene-the 3- and 4-methyltoluene sequence is correct.

The TLSER results suggest that the cubane structure is more like the alkanes than the aromatics. The average TLSER based difference, $\Delta_{\mathrm{a}} \mathrm{H}$ (alkane) $-\Delta_{\mathrm{a}} \mathrm{H}$ (nitroalkane), for the pairsmethane, nitromethane; ethane, nitroethane; propane, $2-$ nitropropane; cyclopropane, nitrocyclopropane; and 2,2dimethylpropane, nitro-2,2-dimethylpropane-is $233 \mathrm{~kJ} \mathrm{~mol}^{-1}$ which agrees very well with their corresponding empirical average difference of $240 \mathrm{~kJ} \mathrm{~mol}^{-1}$. The TLSER average difference for aromatic-nitroaromatic pairs-benzene, nitrobenzene and toluene with the $2-, 3$ - and 4 -nitrotoluenes-is $124 \mathrm{~kJ} \mathrm{~mol}^{-1}$ which agrees very well with their corresponding empirical average difference of $123 \mathrm{~kJ} \mathrm{~mol}^{-1}$. Thus, the cubane-nitrocubane TLSER calculated difference of $242 \mathrm{~kJ} \mathrm{~mol}^{-1}$ agrees very well with the alkane-nitroalkane difference. In fact, the TLSER predicted value for cubane is $1704.1 \mathrm{~kJ} \mathrm{~mol}^{-1}$ which is close to the $1700 \mathrm{~kJ} \mathrm{~mol}^{-1}$ estimated by R itchie and Bacharach ${ }^{1}$ from ab initio techniques. The TLSER predicted acidities for cubanenitrocubane are different from acidities calculated directly. Table 4 shows differences in $\Delta_{\mathrm{a}} \mathrm{H}$ predicted from MNDO (ca. $74 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ), from PM $3\left(94 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ and from A M 1 (ca. 77 kJ $\mathrm{mol}^{-1}$ ). The difference from $6-31+\mathrm{G}$ direct calculations is ca. $121 \mathrm{~kJ} \mathrm{~mol}^{-1}$. If these differences were obtained from the correlation equations in Table 5, these last differences would be scaled smaller by the factor of the corresponding slope
We turn to other compounds (besides cubane) for which no empirical $\Delta_{\mathrm{a}} \mathrm{H}$ values were available. Nitramine and dinitramide had empirical $\Delta_{\mathrm{a}} \mathrm{G}$ values only; these are 1415.4 and 1242.6 kJ $\mathrm{mol}^{-1}$, respectively. The $\Delta_{\mathrm{a}} \mathrm{G}$ TLSER regression, eqn. (7a) in Table 6, predicts 1429.2 and $1234.6 \mathrm{~kJ} \mathrm{~mol}^{-1}$, respectively. The TLSER $\Delta_{\mathrm{a}} \mathrm{H}$ predicted values [eqn. (7), Table 6] are 1458.3 and $1260.5 \mathrm{~kJ} \mathrm{~mol}^{-1}$, respectively. Consequently, the T $\Delta \mathrm{S}$ terms are consistent with empirical values. This predicts the dinitramide to be the most acidic of the compounds in this set. For 2methyltoluene, the TLSER predicted $\Delta_{\mathrm{a}} \mathrm{H}$ value is similar to those predicted for the 3 - and 4 -methyltoluenes. The predicted (empirical value not available) but-2-ene value ( 1652.3 kJ $\mathrm{mol}^{-1}$ ) is close to the predicted value for but-1-ene ( 1655.2 kJ $\mathrm{mol}^{-1}$ ). H owever, as one referee pointed out, this comparison raises questions regarding the but-2-ene isomer and the anion involved. The TLSER parameter calculations in eqn. (7) refer to the neutral molecule and say nothing about the anion. H owever, the (E)-but-2-ene isomer TLSER parameters were used since it is morestablethan the ( $Z$ )-but-2-ene isomer as indicated by the MNDO heat of formation values. The referee pointed out that the E -form is more stable than the Z -form by ca. 7 kJ $\mathrm{mol}^{-1}$ and more stable than but-1-ene by ca. $11 \mathrm{~kJ} \mathrm{~mol}{ }^{-1}$; this is in keeping with Solomons. ${ }^{24}$ For the most part, the acidities have been taken as referring to the most stable molecule going to the most stable anion; this appears to be the E -form of the but-2-ene ion. The predicted cycloocta-1,4-diene value is close to that of the predicted cycloocta-1,3-diene. A gain, the TLSER predicts nitropropane to be similar in acidity to 2 nitropropane. Trinitromethane is predicted to be less acidic than dinitramide but much more acidic than nitromethane as would be expected.

Table 6 shows that triphenylcyclopropane, cyclopentadiene and $\mathrm{NH}_{3}$ are outliers; these are only three out of the 89 selected compounds with empirical $\Delta_{a} \mathrm{H}$ values. Removing these increased statistical significance but did not remove any descriptors. $\mathrm{NH}_{3}$ is a small molecule and MNDO does not describe it well; removing it increased the statistical significance of the volumeterm. Considering the very good empirical preci-
sion and, hence, the likely good accuracy, it is difficult to suggest that the three outliers have poor empirical values. A s they become available, more cyclic unstrained (but not aromatic) compounds should be included in correlation studies to help understand why the other two molecules are outliers.

## Conclusion

At the computational levels used here, directly calculated $\Delta_{\mathrm{a}} \mathrm{H}$ values are not as close to the empirical values as one would like. H owever, a correlation equation between the empirical and calculated values provides improved fit and, hence, prediction. The $6-31+G$ equation [eqn. (3)] gives a better empirical to calculated fit, as evidenced by accounting for more of the variance, 0.992 , than do those for the AM 1, M ND O, PM 3 and TLSER approaches. A $n$ advantage of the direct methods is that the calculations are straightforward for the parent molecule and the anion. A disadvantage is that the semiempirical results do not fit empirical values well, while the ab initio approach requires much more computer time for the higher order calculations necessary for a better fit. A s was mentioned in the Introduction, the latter may present convergence problems. If empirical data are available, a correlation equation between directly calculated and empirical values can be used to improve the fit.
The TLSER correlation equations make good physical sense; $\Delta_{\mathrm{a}} \mathrm{H}$ and $\Delta_{\mathrm{a}} \mathrm{G}$ increase with basicity and decrease with acidity descriptors. The TLSER equation gives a respectable calculated to empirical value fit as evidenced by accounting for 0.846 of the $\Delta_{\mathrm{a}} \mathrm{H}$ variance. The SD value of 41 deviation makes it difficult to predict trends in acidity for compounds that have similar values. An advantage of the TLSER method is that once the correlation equation is found, calculations only have to be done on the molecule. A disadvantage is that a statistically valid set of empirical values must be known in order to get this correlation equation. A further drawback is that the equation only applies to types of compounds used in deriving it.
The reasonable gas phase acidity values for the nitro compounds suggest possible usefulness of the TLSER approach in studying other properties of these energetic materials.

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[^0]:    ${ }^{\text {a }} \AA=\AA$ ngstrom; heV $=$ hecto-electronvolt ( $1 \mathrm{heV}=10^{2} \mathrm{eV}=9.6485 \times 10^{3} \mathrm{~kJ} \mathrm{~mol}{ }^{-1}$ ); acu=atomic charge unit; $\mathrm{HB}=$ hydrogen bond; $\mathrm{E}_{1}=\mathrm{LU} \mathrm{M} 0$

